

Orthogonal Projection Shifted Derivative Filters on the BCC Lattice

Definitions of the Building Block Functions

■ Helper functions and definitions of 1D B-splines

```
R = 1 / 2 * {{1, -1, -1, 1}, {-1, 1, -1, 1}, {-1, -1, 1, 1}, {1, 1, 1, 1}};

Sbs[n_, x_] := InverseFourierTransform[ $\left(\frac{1 - \text{Exp}[-I * w]}{I * w}\right)^{n+1}$ , w, x, FourierParameters -> {1, -1}];

Box0[x_] = FullSimplify[Sbs[0, x]];
Tent[x_] = FullSimplify[Sbs[1, x]];
Quad[x_] = FullSimplify[Sbs[2, x]];
Cubic[x_] = FullSimplify[Sbs[3, x]];
Quartic[x_] = FullSimplify[Sbs[4, x]];
Tentprime[x_] = FullSimplify[Box0[x] - Box0[x - 1]];
Quadprime[x_] = FullSimplify[Tent[x] - Tent[x - 1]];
Cubicprime[x_] = FullSimplify[Quad[x] - Quad[x - 1]];
Quarticprime[x_] = FullSimplify[Cubic[x] - Cubic[x - 1]];
```

■ Linear, Quintic, Nonic, Tredecic and Septendecic Box Splines

```
Lbs[x_, y_, z_] := 4 * Integrate[ $\frac{1}{16}$  Product[Box0[ $\frac{1}{2}$  * R[[k]] * {x, y, z, w}], {k, 1, 4}], {w, 0, 4}];

Qbs[x_, y_, z_] := 4 * Integrate[ $\frac{1}{16}$  Product[Tent[ $\frac{1}{2}$  * R[[k]] * {x, y, z, w}], {k, 1, 4}], {w, 0, 8}];

Nbs[x_, y_, z_] :=
  4 * Integrate[ $\frac{1}{16}$  Product[Quad[ $\frac{1}{2}$  * R[[k]] * {x, y, z, w}], {k, 1, 4}], {w, 0, 12}];

Tdbb[x_, y_, z_] :=
  4 * Integrate[ $\frac{1}{16}$  Product[Cubic[ $\frac{1}{2}$  * R[[k]] * {x, y, z, w}], {k, 1, 4}], {w, 0, 16}];

Sdbb[x_, y_, z_] :=
  4 * Integrate[ $\frac{1}{16}$  Product[Quartic[ $\frac{1}{2}$  * R[[k]] * {x, y, z, w}], {k, 1, 4}], {w, 0, 20}];
```

A function that generates BCC points within the bounding box $[-n, n]^3$

```
BCCpoints[n_] :=
  Select[Tuples[Range[-n, n], 3], (EvenQ[#[[1]]] && EvenQ[#[[2]]] && EvenQ[#[[3]]]) ||
    (OddQ[#[[1]]] && OddQ[#[[2]]] && OddQ[#[[3]]]) &];
```

Directional Derivative Filters

Filters that orthogonally project the directional derivative of a first stage approximation. To recover the gradient, we need to compute directional derivatives along the three principle directions of the BCC lattice.

■ Directional Derivatives of a Nonic Box Spline orthogonally projected onto shifted Quintic Box Splines (NQs)

For each directional derivative, we need a different type of shift.

Each can be computed by shifting the directional derivative of a Tredecic Box Spline (generated by Cubic B - Splines)

```
CdNQ[x_, y_, z_, i_] :=
  
$$\frac{4}{16} * \text{Integrate}\left[\text{Sum}\left[\text{Quarticprime}\left[\frac{1}{2} * R[[j]] \cdot \{x, y, z, w\}\right] * \frac{1}{2} R[[j]][[i]] * \text{Product}\left[\text{Quartic}\left[\frac{1}{2} * R[[k]] \cdot \{x, y, z, w\}\right], \{k, \text{Select}[\{1, 2, 3, 4\}, \# \neq j \&]\}, \{j, 1, 4\}\right], \{w, 0, 20\}\right];$$


CdNQ1[x_, y_, z_] := CdNQ[x, y, z, 1] - CdNQ[x, y, z, 2] - CdNQ[x, y, z, 3];
CdNQ2[x_, y_, z_] := -CdNQ[x, y, z, 1] + CdNQ[x, y, z, 2] - CdNQ[x, y, z, 3];
CdNQ3[x_, y_, z_] := -CdNQ[x, y, z, 1] - CdNQ[x, y, z, 2] + CdNQ[x, y, z, 3];
```

Shifts for the different directions

```
shift =  $\left\{\frac{1}{2}\{1, -1, -1\}, \frac{1}{2}\{-1, 1, -1\}, \frac{1}{2}\{-1, -1, 1\}\right\};$ 

DdNQ1 =
  Select[ $\{\#, \text{CdNQ1}[\#[[1]] + \text{shift}[[1, 1]], \#[[2]] + \text{shift}[[1, 2]], \#[[3]] + \text{shift}[[1, 3]]]\}$  & /@
    BCCpoints[10],  $\#[[2]] \neq 0 \&$ ];
DdNQ2 = Select[ $\{\#, \text{CdNQ2}[\#[[1]] + \text{shift}[[2, 1]], \#[[2]] + \text{shift}[[2, 2]], \#[[3]] + \text{shift}[[2, 3]]]\}$  & /@ BCCpoints[10],  $\#[[2]] \neq 0 \&$ ];
DdNQ3 = Select[ $\{\#, \text{CdNQ3}[\#[[1]] + \text{shift}[[3, 1]], \#[[2]] + \text{shift}[[3, 2]], \#[[3]] + \text{shift}[[3, 3]]]\}$  & /@ BCCpoints[10],  $\#[[2]] \neq 0 \&$ ];
```

■ Directional Derivatives of a Quintic Box Spline orthogonally projected onto a shifted Quintic Box Splines (QQs)

```
CdQQ[x_, y_, z_, i_] :=
  
$$\frac{4}{16} * \text{Integrate}\left[\text{Sum}\left[\text{Cubicprime}\left[\frac{1}{2} * R[[j]] \cdot \{x, y, z, w\}\right] * \frac{1}{2} R[[j]][[i]] * \text{Product}\left[\text{Cubic}\left[\frac{1}{2} * R[[k]] \cdot \{x, y, z, w\}\right], \{k, \text{Select}[\{1, 2, 3, 4\}, \# \neq j \&]\}, \{j, 1, 4\}\right], \{w, 0, 16\}\right];$$


CdQQ1[x_, y_, z_] := CdQQ[x, y, z, 1] - CdQQ[x, y, z, 2] - CdQQ[x, y, z, 3];
CdQQ2[x_, y_, z_] := -CdQQ[x, y, z, 1] + CdQQ[x, y, z, 2] - CdQQ[x, y, z, 3];
CdQQ3[x_, y_, z_] := -CdQQ[x, y, z, 1] - CdQQ[x, y, z, 2] + CdQQ[x, y, z, 3];
DdQQ1 =
  Select[ $\{\#, \text{CdQQ1}[\#[[1]] + \text{shift}[[1, 1]], \#[[2]] + \text{shift}[[1, 2]], \#[[3]] + \text{shift}[[1, 3]]]\}$  & /@
    BCCpoints[8],  $\#[[2]] \neq 0 \&$ ];
DdQQ2 = Select[ $\{\#, \text{CdQQ2}[\#[[1]] + \text{shift}[[2, 1]], \#[[2]] + \text{shift}[[2, 2]], \#[[3]] + \text{shift}[[2, 3]]]\}$  & /@ BCCpoints[8],  $\#[[2]] \neq 0 \&$ ];
DdQQ3 = Select[ $\{\#, \text{CdQQ3}[\#[[1]] + \text{shift}[[3, 1]], \#[[2]] + \text{shift}[[3, 2]], \#[[3]] + \text{shift}[[3, 3]]]\}$  & /@ BCCpoints[8],  $\#[[2]] \neq 0 \&$ ];
```

```

Export["DdQQ1.mat", Flatten[#] & /@ DdQQ1, "Mat"];
Export["DdQQ2.mat", Flatten[#] & /@ DdQQ2, "Mat"];
Export["DdQQ3.mat", Flatten[#] & /@ DdQQ3, "Mat"];
Export["DdNQ1.mat", Flatten[#] & /@ DdNQ1, "Mat"];
Export["DdNQ2.mat", Flatten[#] & /@ DdNQ2, "Mat"];
Export["DdNQ3.mat", Flatten[#] & /@ DdNQ3, "Mat"];

```

DdQQ1

$$\begin{aligned}
& \left\{ \{-7, 1, 1\}, \frac{25}{4904976384} \right\}, \left\{ \{-6, 0, 0\}, \frac{1829}{875888640} \right\}, \left\{ \{-6, 0, 2\}, \frac{2153}{4904976384} \right\}, \\
& \left\{ \{-6, 2, 0\}, \frac{2153}{4904976384} \right\}, \left\{ \{-6, 2, 2\}, \frac{1487}{24524881920} \right\}, \left\{ \{-5, -1, -1\}, \frac{1663}{1362493440} \right\}, \\
& \left\{ \{-5, -1, 1\}, \frac{264307}{6131220480} \right\}, \left\{ \{-5, -1, 3\}, \frac{20467}{24524881920} \right\}, \left\{ \{-5, 1, -1\}, \frac{264307}{6131220480} \right\}, \\
& \left\{ \{-5, 1, 1\}, \frac{8221823}{24524881920} \right\}, \left\{ \{-5, 1, 3\}, \frac{35267}{8174960640} \right\}, \left\{ \{-5, 3, -1\}, \frac{20467}{24524881920} \right\}, \\
& \left\{ \{-5, 3, 1\}, \frac{35267}{8174960640} \right\}, \left\{ \{-5, 3, 3\}, \frac{1007}{24524881920} \right\}, \left\{ \{-4, -2, -2\}, -\frac{19709}{6131220480} \right\}, \\
& \left\{ \{-4, -2, 0\}, \frac{21773}{4087480320} \right\}, \left\{ \{-4, -2, 2\}, \frac{294541}{6131220480} \right\}, \left\{ \{-4, -2, 4\}, \frac{487}{4904976384} \right\}, \\
& \left\{ \{-4, 0, -2\}, \frac{21773}{4087480320} \right\}, \left\{ \{-4, 0, 0\}, \frac{11016701}{4087480320} \right\}, \left\{ \{-4, 0, 2\}, \frac{81959}{35389440} \right\}, \\
& \left\{ \{-4, 0, 4\}, \frac{6943}{908328960} \right\}, \left\{ \{-4, 2, -2\}, \frac{294541}{6131220480} \right\}, \left\{ \{-4, 2, 0\}, \frac{81959}{35389440} \right\}, \\
& \left\{ \{-4, 2, 2\}, \frac{31775213}{24524881920} \right\}, \left\{ \{-4, 2, 4\}, \frac{21001}{8174960640} \right\}, \left\{ \{-4, 4, -2\}, \frac{487}{4904976384} \right\}, \\
& \left\{ \{-4, 4, 0\}, \frac{6943}{908328960} \right\}, \left\{ \{-4, 4, 2\}, \frac{21001}{8174960640} \right\}, \left\{ \{-4, 4, 4\}, \frac{1}{1167851520} \right\}, \\
& \left\{ \{-3, -3, -3\}, -\frac{487}{4904976384} \right\}, \left\{ \{-3, -3, -1\}, -\frac{294541}{6131220480} \right\}, \\
& \left\{ \{-3, -3, 1\}, -\frac{21773}{4087480320} \right\}, \left\{ \{-3, -3, 3\}, \frac{19709}{6131220480} \right\}, \left\{ \{-3, -1, -3\}, -\frac{294541}{6131220480} \right\}, \\
& \left\{ \{-3, -1, -1\}, -\frac{19866733}{12262440960} \right\}, \left\{ \{-3, -1, 1\}, \frac{28959439}{4087480320} \right\}, \left\{ \{-3, -1, 3\}, \frac{34402589}{24524881920} \right\}, \\
& \left\{ \{-3, -1, 5\}, \frac{20467}{24524881920} \right\}, \left\{ \{-3, 1, -3\}, -\frac{21773}{4087480320} \right\}, \left\{ \{-3, 1, -1\}, \frac{28959439}{4087480320} \right\}, \\
& \left\{ \{-3, 1, 1\}, \frac{102820547}{2724986880} \right\}, \left\{ \{-3, 1, 3\}, \frac{46791673}{8174960640} \right\}, \left\{ \{-3, 1, 5\}, \frac{35267}{8174960640} \right\},
\end{aligned}$$

$$\begin{aligned}
& \left\{ \{-3, 3, -3\}, \frac{19709}{6131220480} \right\}, \left\{ \{-3, 3, -1\}, \frac{34402589}{24524881920} \right\}, \left\{ \{-3, 3, 1\}, \frac{46791673}{8174960640} \right\}, \\
& \left\{ \{-3, 3, 3\}, \frac{3451487}{8174960640} \right\}, \left\{ \{-3, 3, 5\}, \frac{1007}{24524881920} \right\}, \left\{ \{-3, 5, -1\}, \frac{20467}{24524881920} \right\}, \\
& \left\{ \{-3, 5, 1\}, \frac{35267}{8174960640} \right\}, \left\{ \{-3, 5, 3\}, \frac{1007}{24524881920} \right\}, \left\{ \{-2, -4, -2\}, -\frac{20467}{24524881920} \right\}, \\
& \left\{ \{-2, -4, 0\}, -\frac{264307}{6131220480} \right\}, \left\{ \{-2, -4, 2\}, -\frac{1663}{1362493440} \right\}, \left\{ \{-2, -2, -4\}, -\frac{20467}{24524881920} \right\}, \\
& \left\{ \{-2, -2, -2\}, -\frac{34402589}{24524881920} \right\}, \left\{ \{-2, -2, 0\}, -\frac{28959439}{4087480320} \right\}, \left\{ \{-2, -2, 2\}, \frac{19866733}{12262440960} \right\}, \\
& \left\{ \{-2, -2, 4\}, \frac{294541}{6131220480} \right\}, \left\{ \{-2, 0, -4\}, -\frac{264307}{6131220480} \right\}, \left\{ \{-2, 0, -2\}, -\frac{28959439}{4087480320} \right\}, \\
& \left\{ \{-2, 0, 0\}, \frac{4219589}{222953472} \right\}, \left\{ \{-2, 0, 2\}, \frac{1280877911}{24524881920} \right\}, \left\{ \{-2, 0, 4\}, \frac{81959}{35389440} \right\}, \\
& \left\{ \{-2, 0, 6\}, \frac{2153}{4904976384} \right\}, \left\{ \{-2, 2, -4\}, -\frac{1663}{1362493440} \right\}, \left\{ \{-2, 2, -2\}, \frac{19866733}{12262440960} \right\}, \\
& \left\{ \{-2, 2, 0\}, \frac{1280877911}{24524881920} \right\}, \left\{ \{-2, 2, 2\}, \frac{382327747}{8174960640} \right\}, \left\{ \{-2, 2, 4\}, \frac{31775213}{24524881920} \right\}, \\
& \left\{ \{-2, 2, 6\}, \frac{1487}{24524881920} \right\}, \left\{ \{-2, 4, -2\}, \frac{294541}{6131220480} \right\}, \left\{ \{-2, 4, 0\}, \frac{81959}{35389440} \right\}, \\
& \left\{ \{-2, 4, 2\}, \frac{31775213}{24524881920} \right\}, \left\{ \{-2, 4, 4\}, \frac{21001}{8174960640} \right\}, \left\{ \{-2, 6, 0\}, \frac{2153}{4904976384} \right\}, \\
& \left\{ \{-2, 6, 2\}, \frac{1487}{24524881920} \right\}, \left\{ \{-1, -5, -1\}, -\frac{2153}{4904976384} \right\}, \left\{ \{-1, -5, 1\}, -\frac{1829}{875888640} \right\}, \\
& \left\{ \{-1, -3, -3\}, -\frac{6943}{908328960} \right\}, \left\{ \{-1, -3, -1\}, -\frac{81959}{35389440} \right\}, \left\{ \{-1, -3, 1\}, -\frac{11016701}{4087480320} \right\}, \\
& \left\{ \{-1, -3, 3\}, -\frac{21773}{4087480320} \right\}, \left\{ \{-1, -1, -5\}, -\frac{2153}{4904976384} \right\}, \left\{ \{-1, -1, -3\}, -\frac{81959}{35389440} \right\}, \\
& \left\{ \{-1, -1, -1\}, -\frac{1280877911}{24524881920} \right\}, \left\{ \{-1, -1, 1\}, -\frac{4219589}{222953472} \right\}, \left\{ \{-1, -1, 3\}, \frac{28959439}{4087480320} \right\}, \\
& \left\{ \{-1, -1, 5\}, \frac{264307}{6131220480} \right\}, \left\{ \{-1, 1, -5\}, -\frac{1829}{875888640} \right\}, \left\{ \{-1, 1, -3\}, -\frac{11016701}{4087480320} \right\}, \\
& \left\{ \{-1, 1, -1\}, -\frac{4219589}{222953472} \right\}, \left\{ \{-1, 1, 1\}, \frac{139391293}{1167851520} \right\}, \left\{ \{-1, 1, 3\}, \frac{102820547}{2724986880} \right\}, \\
& \left\{ \{-1, 1, 5\}, \frac{8221823}{24524881920} \right\}, \left\{ \{-1, 1, 7\}, \frac{25}{4904976384} \right\}, \left\{ \{-1, 3, -3\}, -\frac{21773}{4087480320} \right\},
\end{aligned}$$

$$\begin{aligned}
& \left\{ \{-1, 3, -1\}, \frac{28\,959\,439}{4\,087\,480\,320} \right\}, \left\{ \{-1, 3, 1\}, \frac{102\,820\,547}{2\,724\,986\,880} \right\}, \left\{ \{-1, 3, 3\}, \frac{46\,791\,673}{8\,174\,960\,640} \right\}, \\
& \left\{ \{-1, 3, 5\}, \frac{35\,267}{8\,174\,960\,640} \right\}, \left\{ \{-1, 5, -1\}, \frac{264\,307}{6\,131\,220\,480} \right\}, \left\{ \{-1, 5, 1\}, \frac{8\,221\,823}{24\,524\,881\,920} \right\}, \\
& \left\{ \{-1, 5, 3\}, \frac{35\,267}{8\,174\,960\,640} \right\}, \left\{ \{-1, 7, 1\}, \frac{25}{4\,904\,976\,384} \right\}, \left\{ \{0, -6, 0\}, -\frac{25}{4\,904\,976\,384} \right\}, \\
& \left\{ \{0, -4, -2\}, -\frac{35\,267}{8\,174\,960\,640} \right\}, \left\{ \{0, -4, 0\}, -\frac{8\,221\,823}{24\,524\,881\,920} \right\}, \left\{ \{0, -4, 2\}, -\frac{264\,307}{6\,131\,220\,480} \right\}, \\
& \left\{ \{0, -2, -4\}, -\frac{35\,267}{8\,174\,960\,640} \right\}, \left\{ \{0, -2, -2\}, -\frac{46\,791\,673}{8\,174\,960\,640} \right\}, \left\{ \{0, -2, 0\}, -\frac{102\,820\,547}{2\,724\,986\,880} \right\}, \\
& \left\{ \{0, -2, 2\}, -\frac{28\,959\,439}{4\,087\,480\,320} \right\}, \left\{ \{0, -2, 4\}, \frac{21\,773}{4\,087\,480\,320} \right\}, \left\{ \{0, 0, -6\}, -\frac{25}{4\,904\,976\,384} \right\}, \\
& \left\{ \{0, 0, -4\}, -\frac{8\,221\,823}{24\,524\,881\,920} \right\}, \left\{ \{0, 0, -2\}, -\frac{102\,820\,547}{2\,724\,986\,880} \right\}, \left\{ \{0, 0, 0\}, -\frac{139\,391\,293}{1\,167\,851\,520} \right\}, \\
& \left\{ \{0, 0, 2\}, \frac{4\,219\,589}{222\,953\,472} \right\}, \left\{ \{0, 0, 4\}, \frac{11\,016\,701}{4\,087\,480\,320} \right\}, \left\{ \{0, 0, 6\}, \frac{1829}{875\,888\,640} \right\}, \\
& \left\{ \{0, 2, -4\}, -\frac{264\,307}{6\,131\,220\,480} \right\}, \left\{ \{0, 2, -2\}, -\frac{28\,959\,439}{4\,087\,480\,320} \right\}, \left\{ \{0, 2, 0\}, \frac{4\,219\,589}{222\,953\,472} \right\}, \\
& \left\{ \{0, 2, 2\}, \frac{1\,280\,877\,911}{24\,524\,881\,920} \right\}, \left\{ \{0, 2, 4\}, \frac{81\,959}{35\,389\,440} \right\}, \left\{ \{0, 2, 6\}, \frac{2153}{4\,904\,976\,384} \right\}, \\
& \left\{ \{0, 4, -2\}, \frac{21\,773}{4\,087\,480\,320} \right\}, \left\{ \{0, 4, 0\}, \frac{11\,016\,701}{4\,087\,480\,320} \right\}, \left\{ \{0, 4, 2\}, \frac{81\,959}{35\,389\,440} \right\}, \\
& \left\{ \{0, 4, 4\}, \frac{6943}{908\,328\,960} \right\}, \left\{ \{0, 6, 0\}, \frac{1829}{875\,888\,640} \right\}, \left\{ \{0, 6, 2\}, \frac{2153}{4\,904\,976\,384} \right\}, \\
& \left\{ \{1, -5, -1\}, -\frac{1487}{24\,524\,881\,920} \right\}, \left\{ \{1, -5, 1\}, -\frac{2153}{4\,904\,976\,384} \right\}, \left\{ \{1, -3, -3\}, -\frac{21\,001}{8\,174\,960\,640} \right\}, \\
& \left\{ \{1, -3, -1\}, -\frac{31\,775\,213}{24\,524\,881\,920} \right\}, \left\{ \{1, -3, 1\}, -\frac{81\,959}{35\,389\,440} \right\}, \left\{ \{1, -3, 3\}, -\frac{294\,541}{6\,131\,220\,480} \right\}, \\
& \left\{ \{1, -1, -5\}, -\frac{1487}{24\,524\,881\,920} \right\}, \left\{ \{1, -1, -3\}, -\frac{31\,775\,213}{24\,524\,881\,920} \right\}, \left\{ \{1, -1, -1\}, -\frac{382\,327\,747}{8\,174\,960\,640} \right\}, \\
& \left\{ \{1, -1, 1\}, -\frac{1\,280\,877\,911}{24\,524\,881\,920} \right\}, \left\{ \{1, -1, 3\}, -\frac{19\,866\,733}{12\,262\,440\,960} \right\}, \left\{ \{1, -1, 5\}, \frac{1663}{1\,362\,493\,440} \right\}, \\
& \left\{ \{1, 1, -5\}, -\frac{2153}{4\,904\,976\,384} \right\}, \left\{ \{1, 1, -3\}, -\frac{81\,959}{35\,389\,440} \right\}, \left\{ \{1, 1, -1\}, -\frac{1\,280\,877\,911}{24\,524\,881\,920} \right\}, \\
& \left\{ \{1, 1, 1\}, -\frac{4\,219\,589}{222\,953\,472} \right\}, \left\{ \{1, 1, 3\}, \frac{28\,959\,439}{4\,087\,480\,320} \right\}, \left\{ \{1, 1, 5\}, \frac{264\,307}{6\,131\,220\,480} \right\},
\end{aligned}$$

$$\begin{aligned}
& \left\{ \{1, 3, -3\}, -\frac{294541}{6131220480} \right\}, \left\{ \{1, 3, -1\}, -\frac{19866733}{12262440960} \right\}, \left\{ \{1, 3, 1\}, \frac{28959439}{4087480320} \right\}, \\
& \left\{ \{1, 3, 3\}, \frac{34402589}{24524881920} \right\}, \left\{ \{1, 3, 5\}, \frac{20467}{24524881920} \right\}, \left\{ \{1, 5, -1\}, \frac{1663}{1362493440} \right\}, \\
& \left\{ \{1, 5, 1\}, \frac{264307}{6131220480} \right\}, \left\{ \{1, 5, 3\}, \frac{20467}{24524881920} \right\}, \left\{ \{2, -4, -2\}, -\frac{1007}{24524881920} \right\}, \\
& \left\{ \{2, -4, 0\}, -\frac{35267}{8174960640} \right\}, \left\{ \{2, -4, 2\}, -\frac{20467}{24524881920} \right\}, \left\{ \{2, -2, -4\}, -\frac{1007}{24524881920} \right\}, \\
& \left\{ \{2, -2, -2\}, -\frac{3451487}{8174960640} \right\}, \left\{ \{2, -2, 0\}, -\frac{46791673}{8174960640} \right\}, \left\{ \{2, -2, 2\}, -\frac{34402589}{24524881920} \right\}, \\
& \left\{ \{2, -2, 4\}, -\frac{19709}{6131220480} \right\}, \left\{ \{2, 0, -4\}, -\frac{35267}{8174960640} \right\}, \left\{ \{2, 0, -2\}, -\frac{46791673}{8174960640} \right\}, \\
& \left\{ \{2, 0, 0\}, -\frac{102820547}{2724986880} \right\}, \left\{ \{2, 0, 2\}, -\frac{28959439}{4087480320} \right\}, \left\{ \{2, 0, 4\}, \frac{21773}{4087480320} \right\}, \\
& \left\{ \{2, 2, -4\}, -\frac{20467}{24524881920} \right\}, \left\{ \{2, 2, -2\}, -\frac{34402589}{24524881920} \right\}, \left\{ \{2, 2, 0\}, -\frac{28959439}{4087480320} \right\}, \\
& \left\{ \{2, 2, 2\}, \frac{19866733}{12262440960} \right\}, \left\{ \{2, 2, 4\}, \frac{294541}{6131220480} \right\}, \left\{ \{2, 4, -2\}, -\frac{19709}{6131220480} \right\}, \\
& \left\{ \{2, 4, 0\}, \frac{21773}{4087480320} \right\}, \left\{ \{2, 4, 2\}, \frac{294541}{6131220480} \right\}, \left\{ \{2, 4, 4\}, \frac{487}{4904976384} \right\}, \\
& \left\{ \{3, -3, -3\}, -\frac{1}{1167851520} \right\}, \left\{ \{3, -3, -1\}, -\frac{21001}{8174960640} \right\}, \left\{ \{3, -3, 1\}, -\frac{6943}{908328960} \right\}, \\
& \left\{ \{3, -3, 3\}, -\frac{487}{4904976384} \right\}, \left\{ \{3, -1, -3\}, -\frac{21001}{8174960640} \right\}, \left\{ \{3, -1, -1\}, -\frac{31775213}{24524881920} \right\}, \\
& \left\{ \{3, -1, 1\}, -\frac{81959}{35389440} \right\}, \left\{ \{3, -1, 3\}, -\frac{294541}{6131220480} \right\}, \left\{ \{3, 1, -3\}, -\frac{6943}{908328960} \right\}, \\
& \left\{ \{3, 1, -1\}, -\frac{81959}{35389440} \right\}, \left\{ \{3, 1, 1\}, -\frac{11016701}{4087480320} \right\}, \left\{ \{3, 1, 3\}, -\frac{21773}{4087480320} \right\}, \\
& \left\{ \{3, 3, -3\}, -\frac{487}{4904976384} \right\}, \left\{ \{3, 3, -1\}, -\frac{294541}{6131220480} \right\}, \left\{ \{3, 3, 1\}, -\frac{21773}{4087480320} \right\}, \\
& \left\{ \{3, 3, 3\}, \frac{19709}{6131220480} \right\}, \left\{ \{4, -2, -2\}, -\frac{1007}{24524881920} \right\}, \left\{ \{4, -2, 0\}, -\frac{35267}{8174960640} \right\}, \\
& \left\{ \{4, -2, 2\}, -\frac{20467}{24524881920} \right\}, \left\{ \{4, 0, -2\}, -\frac{35267}{8174960640} \right\}, \left\{ \{4, 0, 0\}, -\frac{8221823}{24524881920} \right\},
\end{aligned}$$

$$\left\{ \{4, 0, 2\}, -\frac{264\,307}{6\,131\,220\,480} \right\}, \left\{ \{4, 2, -2\}, -\frac{20\,467}{24\,524\,881\,920} \right\}, \left\{ \{4, 2, 0\}, -\frac{264\,307}{6\,131\,220\,480} \right\},$$

$$\left\{ \{4, 2, 2\}, -\frac{1663}{1\,362\,493\,440} \right\}, \left\{ \{5, -1, -1\}, -\frac{1487}{24\,524\,881\,920} \right\}, \left\{ \{5, -1, 1\}, -\frac{2153}{4\,904\,976\,384} \right\},$$

$$\left\{ \{5, 1, -1\}, -\frac{2153}{4\,904\,976\,384} \right\}, \left\{ \{5, 1, 1\}, -\frac{1829}{875\,888\,640} \right\}, \left\{ \{6, 0, 0\}, -\frac{25}{4\,904\,976\,384} \right\}$$

DdQQ2

$$\left\{ \{-6, 0, 0\}, -\frac{25}{4\,904\,976\,384} \right\}, \left\{ \{-5, -1, -1\}, -\frac{2153}{4\,904\,976\,384} \right\},$$

$$\left\{ \{-5, -1, 1\}, -\frac{1829}{875\,888\,640} \right\}, \left\{ \{-5, 1, -1\}, -\frac{1487}{24\,524\,881\,920} \right\}, \left\{ \{-5, 1, 1\}, -\frac{2153}{4\,904\,976\,384} \right\},$$

$$\left\{ \{-4, -2, -2\}, -\frac{20\,467}{24\,524\,881\,920} \right\}, \left\{ \{-4, -2, 0\}, -\frac{264\,307}{6\,131\,220\,480} \right\}, \left\{ \{-4, -2, 2\}, -\frac{1663}{1\,362\,493\,440} \right\},$$

$$\left\{ \{-4, 0, -2\}, -\frac{35\,267}{8\,174\,960\,640} \right\}, \left\{ \{-4, 0, 0\}, -\frac{8\,221\,823}{24\,524\,881\,920} \right\}, \left\{ \{-4, 0, 2\}, -\frac{264\,307}{6\,131\,220\,480} \right\},$$

$$\left\{ \{-4, 2, -2\}, -\frac{1007}{24\,524\,881\,920} \right\}, \left\{ \{-4, 2, 0\}, -\frac{35\,267}{8\,174\,960\,640} \right\}, \left\{ \{-4, 2, 2\}, -\frac{20\,467}{24\,524\,881\,920} \right\},$$

$$\left\{ \{-3, -3, -3\}, -\frac{487}{4\,904\,976\,384} \right\}, \left\{ \{-3, -3, -1\}, -\frac{294\,541}{6\,131\,220\,480} \right\}, \left\{ \{-3, -3, 1\}, -\frac{21\,773}{4\,087\,480\,320} \right\},$$

$$\left\{ \{-3, -3, 3\}, -\frac{19\,709}{6\,131\,220\,480} \right\}, \left\{ \{-3, -1, -3\}, -\frac{6943}{908\,328\,960} \right\}, \left\{ \{-3, -1, -1\}, -\frac{81\,959}{35\,389\,440} \right\},$$

$$\left\{ \{-3, -1, 1\}, -\frac{11\,016\,701}{4\,087\,480\,320} \right\}, \left\{ \{-3, -1, 3\}, -\frac{21\,773}{4\,087\,480\,320} \right\}, \left\{ \{-3, 1, -3\}, -\frac{21\,001}{8\,174\,960\,640} \right\},$$

$$\left\{ \{-3, 1, -1\}, -\frac{31\,775\,213}{24\,524\,881\,920} \right\}, \left\{ \{-3, 1, 1\}, -\frac{81\,959}{35\,389\,440} \right\}, \left\{ \{-3, 1, 3\}, -\frac{294\,541}{6\,131\,220\,480} \right\},$$

$$\left\{ \{-3, 3, -3\}, -\frac{1}{1\,167\,851\,520} \right\}, \left\{ \{-3, 3, -1\}, -\frac{21\,001}{8\,174\,960\,640} \right\}, \left\{ \{-3, 3, 1\}, -\frac{6943}{908\,328\,960} \right\},$$

$$\left\{ \{-3, 3, 3\}, -\frac{487}{4\,904\,976\,384} \right\}, \left\{ \{-2, -4, -2\}, -\frac{19\,709}{6\,131\,220\,480} \right\}, \left\{ \{-2, -4, 0\}, -\frac{21\,773}{4\,087\,480\,320} \right\},$$

$$\left\{ \{-2, -4, 2\}, -\frac{294\,541}{6\,131\,220\,480} \right\}, \left\{ \{-2, -4, 4\}, -\frac{487}{4\,904\,976\,384} \right\}, \left\{ \{-2, -2, -4\}, -\frac{20\,467}{24\,524\,881\,920} \right\},$$

$$\left\{ \{-2, -2, -2\}, -\frac{34\,402\,589}{24\,524\,881\,920} \right\}, \left\{ \{-2, -2, 0\}, -\frac{28\,959\,439}{4\,087\,480\,320} \right\}, \left\{ \{-2, -2, 2\}, -\frac{19\,866\,733}{12\,262\,440\,960} \right\},$$

$$\left\{ \{-2, -2, 4\}, -\frac{294\,541}{6\,131\,220\,480} \right\}, \left\{ \{-2, 0, -4\}, -\frac{35\,267}{8\,174\,960\,640} \right\}, \left\{ \{-2, 0, -2\}, -\frac{46\,791\,673}{8\,174\,960\,640} \right\},$$

$$\begin{aligned}
& \left\{ \{-2, 0, 0\}, -\frac{102820547}{2724986880} \right\}, \left\{ \{-2, 0, 2\}, -\frac{28959439}{4087480320} \right\}, \left\{ \{-2, 0, 4\}, \frac{21773}{4087480320} \right\}, \\
& \left\{ \{-2, 2, -4\}, -\frac{1007}{24524881920} \right\}, \left\{ \{-2, 2, -2\}, -\frac{3451487}{8174960640} \right\}, \left\{ \{-2, 2, 0\}, -\frac{46791673}{8174960640} \right\}, \\
& \left\{ \{-2, 2, 2\}, -\frac{34402589}{24524881920} \right\}, \left\{ \{-2, 2, 4\}, -\frac{19709}{6131220480} \right\}, \left\{ \{-2, 4, -2\}, -\frac{1007}{24524881920} \right\}, \\
& \left\{ \{-2, 4, 0\}, -\frac{35267}{8174960640} \right\}, \left\{ \{-2, 4, 2\}, -\frac{20467}{24524881920} \right\}, \left\{ \{-1, -5, -1\}, \frac{1663}{1362493440} \right\}, \\
& \left\{ \{-1, -5, 1\}, \frac{264307}{6131220480} \right\}, \left\{ \{-1, -5, 3\}, \frac{20467}{24524881920} \right\}, \left\{ \{-1, -3, -3\}, -\frac{294541}{6131220480} \right\}, \\
& \left\{ \{-1, -3, -1\}, -\frac{19866733}{12262440960} \right\}, \left\{ \{-1, -3, 1\}, \frac{28959439}{4087480320} \right\}, \left\{ \{-1, -3, 3\}, \frac{34402589}{24524881920} \right\}, \\
& \left\{ \{-1, -3, 5\}, \frac{20467}{24524881920} \right\}, \left\{ \{-1, -1, -5\}, -\frac{2153}{4904976384} \right\}, \left\{ \{-1, -1, -3\}, -\frac{81959}{35389440} \right\}, \\
& \left\{ \{-1, -1, -1\}, -\frac{1280877911}{24524881920} \right\}, \left\{ \{-1, -1, 1\}, -\frac{4219589}{222953472} \right\}, \left\{ \{-1, -1, 3\}, \frac{28959439}{4087480320} \right\}, \\
& \left\{ \{-1, -1, 5\}, \frac{264307}{6131220480} \right\}, \left\{ \{-1, 1, -5\}, -\frac{1487}{24524881920} \right\}, \left\{ \{-1, 1, -3\}, -\frac{31775213}{24524881920} \right\}, \\
& \left\{ \{-1, 1, -1\}, -\frac{382327747}{8174960640} \right\}, \left\{ \{-1, 1, 1\}, -\frac{1280877911}{24524881920} \right\}, \left\{ \{-1, 1, 3\}, -\frac{19866733}{12262440960} \right\}, \\
& \left\{ \{-1, 1, 5\}, \frac{1663}{1362493440} \right\}, \left\{ \{-1, 3, -3\}, -\frac{21001}{8174960640} \right\}, \left\{ \{-1, 3, -1\}, -\frac{31775213}{24524881920} \right\}, \\
& \left\{ \{-1, 3, 1\}, -\frac{81959}{35389440} \right\}, \left\{ \{-1, 3, 3\}, -\frac{294541}{6131220480} \right\}, \left\{ \{-1, 5, -1\}, -\frac{1487}{24524881920} \right\}, \\
& \left\{ \{-1, 5, 1\}, -\frac{2153}{4904976384} \right\}, \left\{ \{0, -6, 0\}, \frac{1829}{875888640} \right\}, \left\{ \{0, -6, 2\}, \frac{2153}{4904976384} \right\}, \\
& \left\{ \{0, -4, -2\}, \frac{21773}{4087480320} \right\}, \left\{ \{0, -4, 0\}, \frac{11016701}{4087480320} \right\}, \left\{ \{0, -4, 2\}, \frac{81959}{35389440} \right\}, \\
& \left\{ \{0, -4, 4\}, \frac{6943}{908328960} \right\}, \left\{ \{0, -2, -4\}, -\frac{264307}{6131220480} \right\}, \left\{ \{0, -2, -2\}, -\frac{28959439}{4087480320} \right\}, \\
& \left\{ \{0, -2, 0\}, \frac{4219589}{222953472} \right\}, \left\{ \{0, -2, 2\}, \frac{1280877911}{24524881920} \right\}, \left\{ \{0, -2, 4\}, \frac{81959}{35389440} \right\}, \\
& \left\{ \{0, -2, 6\}, \frac{2153}{4904976384} \right\}, \left\{ \{0, 0, -6\}, -\frac{25}{4904976384} \right\}, \left\{ \{0, 0, -4\}, -\frac{8221823}{24524881920} \right\}, \\
& \left\{ \{0, 0, -2\}, -\frac{102820547}{2724986880} \right\}, \left\{ \{0, 0, 0\}, -\frac{139391293}{1167851520} \right\}, \left\{ \{0, 0, 2\}, \frac{4219589}{222953472} \right\},
\end{aligned}$$

$$\begin{aligned}
& \left\{ \{0, 0, 4\}, \frac{11\,016\,701}{4\,087\,480\,320} \right\}, \left\{ \{0, 0, 6\}, \frac{1829}{875\,888\,640} \right\}, \left\{ \{0, 2, -4\}, -\frac{35\,267}{8\,174\,960\,640} \right\}, \\
& \left\{ \{0, 2, -2\}, -\frac{46\,791\,673}{8\,174\,960\,640} \right\}, \left\{ \{0, 2, 0\}, -\frac{102\,820\,547}{2\,724\,986\,880} \right\}, \left\{ \{0, 2, 2\}, -\frac{28\,959\,439}{4\,087\,480\,320} \right\}, \\
& \left\{ \{0, 2, 4\}, \frac{21\,773}{4\,087\,480\,320} \right\}, \left\{ \{0, 4, -2\}, -\frac{35\,267}{8\,174\,960\,640} \right\}, \left\{ \{0, 4, 0\}, -\frac{8\,221\,823}{24\,524\,881\,920} \right\}, \\
& \left\{ \{0, 4, 2\}, -\frac{264\,307}{6\,131\,220\,480} \right\}, \left\{ \{0, 6, 0\}, -\frac{25}{4\,904\,976\,384} \right\}, \left\{ \{1, -7, 1\}, \frac{25}{4\,904\,976\,384} \right\}, \\
& \left\{ \{1, -5, -1\}, \frac{264\,307}{6\,131\,220\,480} \right\}, \left\{ \{1, -5, 1\}, \frac{8\,221\,823}{24\,524\,881\,920} \right\}, \left\{ \{1, -5, 3\}, \frac{35\,267}{8\,174\,960\,640} \right\}, \\
& \left\{ \{1, -3, -3\}, -\frac{21\,773}{4\,087\,480\,320} \right\}, \left\{ \{1, -3, -1\}, \frac{28\,959\,439}{4\,087\,480\,320} \right\}, \left\{ \{1, -3, 1\}, \frac{102\,820\,547}{2\,724\,986\,880} \right\}, \\
& \left\{ \{1, -3, 3\}, \frac{46\,791\,673}{8\,174\,960\,640} \right\}, \left\{ \{1, -3, 5\}, \frac{35\,267}{8\,174\,960\,640} \right\}, \left\{ \{1, -1, -5\}, -\frac{1829}{875\,888\,640} \right\}, \\
& \left\{ \{1, -1, -3\}, -\frac{11\,016\,701}{4\,087\,480\,320} \right\}, \left\{ \{1, -1, -1\}, -\frac{4\,219\,589}{222\,953\,472} \right\}, \left\{ \{1, -1, 1\}, \frac{139\,391\,293}{1\,167\,851\,520} \right\}, \\
& \left\{ \{1, -1, 3\}, \frac{102\,820\,547}{2\,724\,986\,880} \right\}, \left\{ \{1, -1, 5\}, \frac{8\,221\,823}{24\,524\,881\,920} \right\}, \left\{ \{1, -1, 7\}, \frac{25}{4\,904\,976\,384} \right\}, \\
& \left\{ \{1, 1, -5\}, -\frac{2153}{4\,904\,976\,384} \right\}, \left\{ \{1, 1, -3\}, -\frac{81\,959}{35\,389\,440} \right\}, \left\{ \{1, 1, -1\}, -\frac{1\,280\,877\,911}{24\,524\,881\,920} \right\}, \\
& \left\{ \{1, 1, 1\}, -\frac{4\,219\,589}{222\,953\,472} \right\}, \left\{ \{1, 1, 3\}, \frac{28\,959\,439}{4\,087\,480\,320} \right\}, \left\{ \{1, 1, 5\}, \frac{264\,307}{6\,131\,220\,480} \right\}, \\
& \left\{ \{1, 3, -3\}, -\frac{6943}{908\,328\,960} \right\}, \left\{ \{1, 3, -1\}, -\frac{81\,959}{35\,389\,440} \right\}, \left\{ \{1, 3, 1\}, -\frac{11\,016\,701}{4\,087\,480\,320} \right\}, \\
& \left\{ \{1, 3, 3\}, -\frac{21\,773}{4\,087\,480\,320} \right\}, \left\{ \{1, 5, -1\}, -\frac{2153}{4\,904\,976\,384} \right\}, \left\{ \{1, 5, 1\}, -\frac{1829}{875\,888\,640} \right\}, \\
& \left\{ \{2, -6, 0\}, \frac{2153}{4\,904\,976\,384} \right\}, \left\{ \{2, -6, 2\}, \frac{1487}{24\,524\,881\,920} \right\}, \left\{ \{2, -4, -2\}, \frac{294\,541}{6\,131\,220\,480} \right\}, \\
& \left\{ \{2, -4, 0\}, \frac{81\,959}{35\,389\,440} \right\}, \left\{ \{2, -4, 2\}, \frac{31\,775\,213}{24\,524\,881\,920} \right\}, \left\{ \{2, -4, 4\}, \frac{21\,001}{8\,174\,960\,640} \right\}, \\
& \left\{ \{2, -2, -4\}, -\frac{1663}{1\,362\,493\,440} \right\}, \left\{ \{2, -2, -2\}, \frac{19\,866\,733}{12\,262\,440\,960} \right\}, \left\{ \{2, -2, 0\}, \frac{1\,280\,877\,911}{24\,524\,881\,920} \right\}, \\
& \left\{ \{2, -2, 2\}, \frac{382\,327\,747}{8\,174\,960\,640} \right\}, \left\{ \{2, -2, 4\}, \frac{31\,775\,213}{24\,524\,881\,920} \right\}, \left\{ \{2, -2, 6\}, \frac{1487}{24\,524\,881\,920} \right\}, \\
& \left\{ \{2, 0, -4\}, -\frac{264\,307}{6\,131\,220\,480} \right\}, \left\{ \{2, 0, -2\}, -\frac{28\,959\,439}{4\,087\,480\,320} \right\}, \left\{ \{2, 0, 0\}, \frac{4\,219\,589}{222\,953\,472} \right\},
\end{aligned}$$

$$\begin{aligned}
& \left\{ \{2, 0, 2\}, \frac{1280877911}{24524881920} \right\}, \left\{ \{2, 0, 4\}, \frac{81959}{35389440} \right\}, \left\{ \{2, 0, 6\}, \frac{2153}{4904976384} \right\}, \\
& \left\{ \{2, 2, -4\}, -\frac{20467}{24524881920} \right\}, \left\{ \{2, 2, -2\}, -\frac{34402589}{24524881920} \right\}, \left\{ \{2, 2, 0\}, -\frac{28959439}{4087480320} \right\}, \\
& \left\{ \{2, 2, 2\}, \frac{19866733}{12262440960} \right\}, \left\{ \{2, 2, 4\}, \frac{294541}{6131220480} \right\}, \left\{ \{2, 4, -2\}, -\frac{20467}{24524881920} \right\}, \\
& \left\{ \{2, 4, 0\}, -\frac{264307}{6131220480} \right\}, \left\{ \{2, 4, 2\}, -\frac{1663}{1362493440} \right\}, \left\{ \{3, -5, -1\}, \frac{20467}{24524881920} \right\}, \\
& \left\{ \{3, -5, 1\}, \frac{35267}{8174960640} \right\}, \left\{ \{3, -5, 3\}, \frac{1007}{24524881920} \right\}, \left\{ \{3, -3, -3\}, \frac{19709}{6131220480} \right\}, \\
& \left\{ \{3, -3, -1\}, \frac{34402589}{24524881920} \right\}, \left\{ \{3, -3, 1\}, \frac{46791673}{8174960640} \right\}, \left\{ \{3, -3, 3\}, \frac{3451487}{8174960640} \right\}, \\
& \left\{ \{3, -3, 5\}, \frac{1007}{24524881920} \right\}, \left\{ \{3, -1, -3\}, -\frac{21773}{4087480320} \right\}, \left\{ \{3, -1, -1\}, \frac{28959439}{4087480320} \right\}, \\
& \left\{ \{3, -1, 1\}, \frac{102820547}{2724986880} \right\}, \left\{ \{3, -1, 3\}, \frac{46791673}{8174960640} \right\}, \left\{ \{3, -1, 5\}, \frac{35267}{8174960640} \right\}, \\
& \left\{ \{3, 1, -3\}, -\frac{294541}{6131220480} \right\}, \left\{ \{3, 1, -1\}, -\frac{19866733}{12262440960} \right\}, \left\{ \{3, 1, 1\}, \frac{28959439}{4087480320} \right\}, \\
& \left\{ \{3, 1, 3\}, \frac{34402589}{24524881920} \right\}, \left\{ \{3, 1, 5\}, \frac{20467}{24524881920} \right\}, \left\{ \{3, 3, -3\}, -\frac{487}{4904976384} \right\}, \\
& \left\{ \{3, 3, -1\}, -\frac{294541}{6131220480} \right\}, \left\{ \{3, 3, 1\}, -\frac{21773}{4087480320} \right\}, \left\{ \{3, 3, 3\}, \frac{19709}{6131220480} \right\}, \\
& \left\{ \{4, -4, -2\}, \frac{487}{4904976384} \right\}, \left\{ \{4, -4, 0\}, \frac{6943}{908328960} \right\}, \left\{ \{4, -4, 2\}, \frac{21001}{8174960640} \right\}, \\
& \left\{ \{4, -4, 4\}, \frac{1}{1167851520} \right\}, \left\{ \{4, -2, -2\}, \frac{294541}{6131220480} \right\}, \left\{ \{4, -2, 0\}, \frac{81959}{35389440} \right\}, \\
& \left\{ \{4, -2, 2\}, \frac{31775213}{24524881920} \right\}, \left\{ \{4, -2, 4\}, \frac{21001}{8174960640} \right\}, \left\{ \{4, 0, -2\}, \frac{21773}{4087480320} \right\}, \\
& \left\{ \{4, 0, 0\}, \frac{11016701}{4087480320} \right\}, \left\{ \{4, 0, 2\}, \frac{81959}{35389440} \right\}, \left\{ \{4, 0, 4\}, \frac{6943}{908328960} \right\}, \\
& \left\{ \{4, 2, -2\}, -\frac{19709}{6131220480} \right\}, \left\{ \{4, 2, 0\}, \frac{21773}{4087480320} \right\}, \left\{ \{4, 2, 2\}, \frac{294541}{6131220480} \right\}, \\
& \left\{ \{4, 2, 4\}, \frac{487}{4904976384} \right\}, \left\{ \{5, -3, -1\}, \frac{20467}{24524881920} \right\}, \left\{ \{5, -3, 1\}, \frac{35267}{8174960640} \right\}, \\
& \left\{ \{5, -3, 3\}, \frac{1007}{24524881920} \right\}, \left\{ \{5, -1, -1\}, \frac{264307}{6131220480} \right\}, \left\{ \{5, -1, 1\}, \frac{8221823}{24524881920} \right\},
\end{aligned}$$

$$\left\{ \{5, -1, 3\}, \frac{35\,267}{8\,174\,960\,640} \right\}, \left\{ \{5, 1, -1\}, \frac{1663}{1\,362\,493\,440} \right\}, \left\{ \{5, 1, 1\}, \frac{264\,307}{6\,131\,220\,480} \right\},$$

$$\left\{ \{5, 1, 3\}, \frac{20\,467}{24\,524\,881\,920} \right\}, \left\{ \{6, -2, 0\}, \frac{2153}{4\,904\,976\,384} \right\}, \left\{ \{6, -2, 2\}, \frac{1487}{24\,524\,881\,920} \right\},$$

$$\left\{ \{6, 0, 0\}, \frac{1829}{875\,888\,640} \right\}, \left\{ \{6, 0, 2\}, \frac{2153}{4\,904\,976\,384} \right\}, \left\{ \{7, -1, 1\}, \frac{25}{4\,904\,976\,384} \right\}$$

DdQQ3

$$\left\{ \{-6, 0, 0\}, -\frac{25}{4\,904\,976\,384} \right\}, \left\{ \{-5, -1, -1\}, -\frac{2153}{4\,904\,976\,384} \right\},$$

$$\left\{ \{-5, -1, 1\}, -\frac{1487}{24\,524\,881\,920} \right\}, \left\{ \{-5, 1, -1\}, -\frac{1829}{875\,888\,640} \right\}, \left\{ \{-5, 1, 1\}, -\frac{2153}{4\,904\,976\,384} \right\},$$

$$\left\{ \{-4, -2, -2\}, -\frac{20\,467}{24\,524\,881\,920} \right\}, \left\{ \{-4, -2, 0\}, -\frac{35\,267}{8\,174\,960\,640} \right\}, \left\{ \{-4, -2, 2\}, -\frac{1007}{24\,524\,881\,920} \right\},$$

$$\left\{ \{-4, 0, -2\}, -\frac{264\,307}{6\,131\,220\,480} \right\}, \left\{ \{-4, 0, 0\}, -\frac{8\,221\,823}{24\,524\,881\,920} \right\}, \left\{ \{-4, 0, 2\}, -\frac{35\,267}{8\,174\,960\,640} \right\},$$

$$\left\{ \{-4, 2, -2\}, -\frac{1663}{1\,362\,493\,440} \right\}, \left\{ \{-4, 2, 0\}, -\frac{264\,307}{6\,131\,220\,480} \right\}, \left\{ \{-4, 2, 2\}, -\frac{20\,467}{24\,524\,881\,920} \right\},$$

$$\left\{ \{-3, -3, -3\}, -\frac{487}{4\,904\,976\,384} \right\}, \left\{ \{-3, -3, -1\}, -\frac{6943}{908\,328\,960} \right\}, \left\{ \{-3, -3, 1\}, -\frac{21\,001}{8\,174\,960\,640} \right\},$$

$$\left\{ \{-3, -3, 3\}, -\frac{1}{1\,167\,851\,520} \right\}, \left\{ \{-3, -1, -3\}, -\frac{294\,541}{6\,131\,220\,480} \right\}, \left\{ \{-3, -1, -1\}, -\frac{81\,959}{35\,389\,440} \right\},$$

$$\left\{ \{-3, -1, 1\}, -\frac{31\,775\,213}{24\,524\,881\,920} \right\}, \left\{ \{-3, -1, 3\}, -\frac{21\,001}{8\,174\,960\,640} \right\}, \left\{ \{-3, 1, -3\}, -\frac{21\,773}{4\,087\,480\,320} \right\},$$

$$\left\{ \{-3, 1, -1\}, -\frac{11\,016\,701}{4\,087\,480\,320} \right\}, \left\{ \{-3, 1, 1\}, -\frac{81\,959}{35\,389\,440} \right\}, \left\{ \{-3, 1, 3\}, -\frac{6943}{908\,328\,960} \right\},$$

$$\left\{ \{-3, 3, -3\}, \frac{19\,709}{6\,131\,220\,480} \right\}, \left\{ \{-3, 3, -1\}, -\frac{21\,773}{4\,087\,480\,320} \right\}, \left\{ \{-3, 3, 1\}, -\frac{294\,541}{6\,131\,220\,480} \right\},$$

$$\left\{ \{-3, 3, 3\}, -\frac{487}{4\,904\,976\,384} \right\}, \left\{ \{-2, -4, -2\}, -\frac{20\,467}{24\,524\,881\,920} \right\}, \left\{ \{-2, -4, 0\}, -\frac{35\,267}{8\,174\,960\,640} \right\},$$

$$\left\{ \{-2, -4, 2\}, -\frac{1007}{24\,524\,881\,920} \right\}, \left\{ \{-2, -2, -4\}, -\frac{19\,709}{6\,131\,220\,480} \right\}, \left\{ \{-2, -2, -2\}, -\frac{34\,402\,589}{24\,524\,881\,920} \right\},$$

$$\left\{ \{-2, -2, 0\}, -\frac{46\,791\,673}{8\,174\,960\,640} \right\}, \left\{ \{-2, -2, 2\}, -\frac{3\,451\,487}{8\,174\,960\,640} \right\}, \left\{ \{-2, -2, 4\}, -\frac{1007}{24\,524\,881\,920} \right\},$$

$$\left\{ \{-2, 0, -4\}, \frac{21\,773}{4\,087\,480\,320} \right\}, \left\{ \{-2, 0, -2\}, -\frac{28\,959\,439}{4\,087\,480\,320} \right\}, \left\{ \{-2, 0, 0\}, -\frac{102\,820\,547}{2\,724\,986\,880} \right\},$$

$$\begin{aligned}
& \left\{ \{-2, 0, 2\}, -\frac{46\,791\,673}{8\,174\,960\,640} \right\}, \left\{ \{-2, 0, 4\}, -\frac{35\,267}{8\,174\,960\,640} \right\}, \left\{ \{-2, 2, -4\}, \frac{294\,541}{6\,131\,220\,480} \right\}, \\
& \left\{ \{-2, 2, -2\}, \frac{19\,866\,733}{12\,262\,440\,960} \right\}, \left\{ \{-2, 2, 0\}, -\frac{28\,959\,439}{4\,087\,480\,320} \right\}, \left\{ \{-2, 2, 2\}, -\frac{34\,402\,589}{24\,524\,881\,920} \right\}, \\
& \left\{ \{-2, 2, 4\}, -\frac{20\,467}{24\,524\,881\,920} \right\}, \left\{ \{-2, 4, -4\}, \frac{487}{4\,904\,976\,384} \right\}, \left\{ \{-2, 4, -2\}, \frac{294\,541}{6\,131\,220\,480} \right\}, \\
& \left\{ \{-2, 4, 0\}, \frac{21\,773}{4\,087\,480\,320} \right\}, \left\{ \{-2, 4, 2\}, -\frac{19\,709}{6\,131\,220\,480} \right\}, \left\{ \{-1, -5, -1\}, -\frac{2153}{4\,904\,976\,384} \right\}, \\
& \left\{ \{-1, -5, 1\}, -\frac{1487}{24\,524\,881\,920} \right\}, \left\{ \{-1, -3, -3\}, -\frac{294\,541}{6\,131\,220\,480} \right\}, \left\{ \{-1, -3, -1\}, -\frac{81\,959}{35\,389\,440} \right\}, \\
& \left\{ \{-1, -3, 1\}, -\frac{31\,775\,213}{24\,524\,881\,920} \right\}, \left\{ \{-1, -3, 3\}, -\frac{21\,001}{8\,174\,960\,640} \right\}, \left\{ \{-1, -1, -5\}, \frac{1663}{1\,362\,493\,440} \right\}, \\
& \left\{ \{-1, -1, -3\}, -\frac{19\,866\,733}{12\,262\,440\,960} \right\}, \left\{ \{-1, -1, -1\}, -\frac{1\,280\,877\,911}{24\,524\,881\,920} \right\}, \left\{ \{-1, -1, 1\}, -\frac{382\,327\,747}{8\,174\,960\,640} \right\}, \\
& \left\{ \{-1, -1, 3\}, -\frac{31\,775\,213}{24\,524\,881\,920} \right\}, \left\{ \{-1, -1, 5\}, -\frac{1487}{24\,524\,881\,920} \right\}, \left\{ \{-1, 1, -5\}, \frac{264\,307}{6\,131\,220\,480} \right\}, \\
& \left\{ \{-1, 1, -3\}, \frac{28\,959\,439}{4\,087\,480\,320} \right\}, \left\{ \{-1, 1, -1\}, -\frac{4\,219\,589}{222\,953\,472} \right\}, \left\{ \{-1, 1, 1\}, -\frac{1\,280\,877\,911}{24\,524\,881\,920} \right\}, \\
& \left\{ \{-1, 1, 3\}, -\frac{81\,959}{35\,389\,440} \right\}, \left\{ \{-1, 1, 5\}, -\frac{2153}{4\,904\,976\,384} \right\}, \left\{ \{-1, 3, -5\}, \frac{20\,467}{24\,524\,881\,920} \right\}, \\
& \left\{ \{-1, 3, -3\}, \frac{34\,402\,589}{24\,524\,881\,920} \right\}, \left\{ \{-1, 3, -1\}, \frac{28\,959\,439}{4\,087\,480\,320} \right\}, \left\{ \{-1, 3, 1\}, -\frac{19\,866\,733}{12\,262\,440\,960} \right\}, \\
& \left\{ \{-1, 3, 3\}, -\frac{294\,541}{6\,131\,220\,480} \right\}, \left\{ \{-1, 5, -3\}, \frac{20\,467}{24\,524\,881\,920} \right\}, \left\{ \{-1, 5, -1\}, \frac{264\,307}{6\,131\,220\,480} \right\}, \\
& \left\{ \{-1, 5, 1\}, \frac{1663}{1\,362\,493\,440} \right\}, \left\{ \{0, -6, 0\}, -\frac{25}{4\,904\,976\,384} \right\}, \left\{ \{0, -4, -2\}, -\frac{264\,307}{6\,131\,220\,480} \right\}, \\
& \left\{ \{0, -4, 0\}, -\frac{8\,221\,823}{24\,524\,881\,920} \right\}, \left\{ \{0, -4, 2\}, -\frac{35\,267}{8\,174\,960\,640} \right\}, \left\{ \{0, -2, -4\}, \frac{21\,773}{4\,087\,480\,320} \right\}, \\
& \left\{ \{0, -2, -2\}, -\frac{28\,959\,439}{4\,087\,480\,320} \right\}, \left\{ \{0, -2, 0\}, -\frac{102\,820\,547}{2\,724\,986\,880} \right\}, \left\{ \{0, -2, 2\}, -\frac{46\,791\,673}{8\,174\,960\,640} \right\}, \\
& \left\{ \{0, -2, 4\}, -\frac{35\,267}{8\,174\,960\,640} \right\}, \left\{ \{0, 0, -6\}, \frac{1829}{875\,888\,640} \right\}, \left\{ \{0, 0, -4\}, \frac{11\,016\,701}{4\,087\,480\,320} \right\}, \\
& \left\{ \{0, 0, -2\}, \frac{4\,219\,589}{222\,953\,472} \right\}, \left\{ \{0, 0, 0\}, -\frac{139\,391\,293}{1\,167\,851\,520} \right\}, \left\{ \{0, 0, 2\}, -\frac{102\,820\,547}{2\,724\,986\,880} \right\}, \\
& \left\{ \{0, 0, 4\}, -\frac{8\,221\,823}{24\,524\,881\,920} \right\}, \left\{ \{0, 0, 6\}, -\frac{25}{4\,904\,976\,384} \right\}, \left\{ \{0, 2, -6\}, \frac{2153}{4\,904\,976\,384} \right\},
\end{aligned}$$

$$\begin{aligned}
& \left\{ \{0, 2, -4\}, \frac{81959}{35389440} \right\}, \left\{ \{0, 2, -2\}, \frac{1280877911}{24524881920} \right\}, \left\{ \{0, 2, 0\}, \frac{4219589}{222953472} \right\}, \\
& \left\{ \{0, 2, 2\}, -\frac{28959439}{4087480320} \right\}, \left\{ \{0, 2, 4\}, -\frac{264307}{6131220480} \right\}, \left\{ \{0, 4, -4\}, \frac{6943}{908328960} \right\}, \\
& \left\{ \{0, 4, -2\}, \frac{81959}{35389440} \right\}, \left\{ \{0, 4, 0\}, \frac{11016701}{4087480320} \right\}, \left\{ \{0, 4, 2\}, \frac{21773}{4087480320} \right\}, \\
& \left\{ \{0, 6, -2\}, \frac{2153}{4904976384} \right\}, \left\{ \{0, 6, 0\}, \frac{1829}{875888640} \right\}, \left\{ \{1, -5, -1\}, -\frac{1829}{875888640} \right\}, \\
& \left\{ \{1, -5, 1\}, -\frac{2153}{4904976384} \right\}, \left\{ \{1, -3, -3\}, -\frac{21773}{4087480320} \right\}, \left\{ \{1, -3, -1\}, -\frac{11016701}{4087480320} \right\}, \\
& \left\{ \{1, -3, 1\}, -\frac{81959}{35389440} \right\}, \left\{ \{1, -3, 3\}, -\frac{6943}{908328960} \right\}, \left\{ \{1, -1, -5\}, \frac{264307}{6131220480} \right\}, \\
& \left\{ \{1, -1, -3\}, \frac{28959439}{4087480320} \right\}, \left\{ \{1, -1, -1\}, -\frac{4219589}{222953472} \right\}, \left\{ \{1, -1, 1\}, -\frac{1280877911}{24524881920} \right\}, \\
& \left\{ \{1, -1, 3\}, -\frac{81959}{35389440} \right\}, \left\{ \{1, -1, 5\}, -\frac{2153}{4904976384} \right\}, \left\{ \{1, 1, -7\}, \frac{25}{4904976384} \right\}, \\
& \left\{ \{1, 1, -5\}, \frac{8221823}{24524881920} \right\}, \left\{ \{1, 1, -3\}, \frac{102820547}{2724986880} \right\}, \left\{ \{1, 1, -1\}, \frac{139391293}{1167851520} \right\}, \\
& \left\{ \{1, 1, 1\}, -\frac{4219589}{222953472} \right\}, \left\{ \{1, 1, 3\}, -\frac{11016701}{4087480320} \right\}, \left\{ \{1, 1, 5\}, -\frac{1829}{875888640} \right\}, \\
& \left\{ \{1, 3, -5\}, \frac{35267}{8174960640} \right\}, \left\{ \{1, 3, -3\}, \frac{46791673}{8174960640} \right\}, \left\{ \{1, 3, -1\}, \frac{102820547}{2724986880} \right\}, \\
& \left\{ \{1, 3, 1\}, \frac{28959439}{4087480320} \right\}, \left\{ \{1, 3, 3\}, -\frac{21773}{4087480320} \right\}, \left\{ \{1, 5, -3\}, \frac{35267}{8174960640} \right\}, \\
& \left\{ \{1, 5, -1\}, \frac{8221823}{24524881920} \right\}, \left\{ \{1, 5, 1\}, \frac{264307}{6131220480} \right\}, \left\{ \{1, 7, -1\}, \frac{25}{4904976384} \right\}, \\
& \left\{ \{2, -4, -2\}, -\frac{1663}{1362493440} \right\}, \left\{ \{2, -4, 0\}, -\frac{264307}{6131220480} \right\}, \left\{ \{2, -4, 2\}, -\frac{20467}{24524881920} \right\}, \\
& \left\{ \{2, -2, -4\}, \frac{294541}{6131220480} \right\}, \left\{ \{2, -2, -2\}, \frac{19866733}{12262440960} \right\}, \left\{ \{2, -2, 0\}, -\frac{28959439}{4087480320} \right\}, \\
& \left\{ \{2, -2, 2\}, -\frac{34402589}{24524881920} \right\}, \left\{ \{2, -2, 4\}, -\frac{20467}{24524881920} \right\}, \left\{ \{2, 0, -6\}, \frac{2153}{4904976384} \right\}, \\
& \left\{ \{2, 0, -4\}, \frac{81959}{35389440} \right\}, \left\{ \{2, 0, -2\}, \frac{1280877911}{24524881920} \right\}, \left\{ \{2, 0, 0\}, \frac{4219589}{222953472} \right\}, \\
& \left\{ \{2, 0, 2\}, -\frac{28959439}{4087480320} \right\}, \left\{ \{2, 0, 4\}, -\frac{264307}{6131220480} \right\}, \left\{ \{2, 2, -6\}, \frac{1487}{24524881920} \right\},
\end{aligned}$$

$$\begin{aligned}
& \left\{ \{2, 2, -4\}, \frac{31\,775\,213}{24\,524\,881\,920} \right\}, \left\{ \{2, 2, -2\}, \frac{382\,327\,747}{8\,174\,960\,640} \right\}, \left\{ \{2, 2, 0\}, \frac{1\,280\,877\,911}{24\,524\,881\,920} \right\}, \\
& \left\{ \{2, 2, 2\}, \frac{19\,866\,733}{12\,262\,440\,960} \right\}, \left\{ \{2, 2, 4\}, -\frac{1663}{1\,362\,493\,440} \right\}, \left\{ \{2, 4, -4\}, \frac{21\,001}{8\,174\,960\,640} \right\}, \\
& \left\{ \{2, 4, -2\}, \frac{31\,775\,213}{24\,524\,881\,920} \right\}, \left\{ \{2, 4, 0\}, \frac{81\,959}{35\,389\,440} \right\}, \left\{ \{2, 4, 2\}, \frac{294\,541}{6\,131\,220\,480} \right\}, \\
& \left\{ \{2, 6, -2\}, \frac{1487}{24\,524\,881\,920} \right\}, \left\{ \{2, 6, 0\}, \frac{2153}{4\,904\,976\,384} \right\}, \left\{ \{3, -3, -3\}, \frac{19\,709}{6\,131\,220\,480} \right\}, \\
& \left\{ \{3, -3, -1\}, -\frac{21\,773}{4\,087\,480\,320} \right\}, \left\{ \{3, -3, 1\}, -\frac{294\,541}{6\,131\,220\,480} \right\}, \left\{ \{3, -3, 3\}, -\frac{487}{4\,904\,976\,384} \right\}, \\
& \left\{ \{3, -1, -5\}, \frac{20\,467}{24\,524\,881\,920} \right\}, \left\{ \{3, -1, -3\}, \frac{34\,402\,589}{24\,524\,881\,920} \right\}, \left\{ \{3, -1, -1\}, \frac{28\,959\,439}{4\,087\,480\,320} \right\}, \\
& \left\{ \{3, -1, 1\}, -\frac{19\,866\,733}{12\,262\,440\,960} \right\}, \left\{ \{3, -1, 3\}, -\frac{294\,541}{6\,131\,220\,480} \right\}, \left\{ \{3, 1, -5\}, \frac{35\,267}{8\,174\,960\,640} \right\}, \\
& \left\{ \{3, 1, -3\}, \frac{46\,791\,673}{8\,174\,960\,640} \right\}, \left\{ \{3, 1, -1\}, \frac{102\,820\,547}{2\,724\,986\,880} \right\}, \left\{ \{3, 1, 1\}, \frac{28\,959\,439}{4\,087\,480\,320} \right\}, \\
& \left\{ \{3, 1, 3\}, -\frac{21\,773}{4\,087\,480\,320} \right\}, \left\{ \{3, 3, -5\}, \frac{1007}{24\,524\,881\,920} \right\}, \left\{ \{3, 3, -3\}, \frac{3\,451\,487}{8\,174\,960\,640} \right\}, \\
& \left\{ \{3, 3, -1\}, \frac{46\,791\,673}{8\,174\,960\,640} \right\}, \left\{ \{3, 3, 1\}, \frac{34\,402\,589}{24\,524\,881\,920} \right\}, \left\{ \{3, 3, 3\}, \frac{19\,709}{6\,131\,220\,480} \right\}, \\
& \left\{ \{3, 5, -3\}, \frac{1007}{24\,524\,881\,920} \right\}, \left\{ \{3, 5, -1\}, \frac{35\,267}{8\,174\,960\,640} \right\}, \left\{ \{3, 5, 1\}, \frac{20\,467}{24\,524\,881\,920} \right\}, \\
& \left\{ \{4, -2, -4\}, \frac{487}{4\,904\,976\,384} \right\}, \left\{ \{4, -2, -2\}, \frac{294\,541}{6\,131\,220\,480} \right\}, \left\{ \{4, -2, 0\}, \frac{21\,773}{4\,087\,480\,320} \right\}, \\
& \left\{ \{4, -2, 2\}, -\frac{19\,709}{6\,131\,220\,480} \right\}, \left\{ \{4, 0, -4\}, \frac{6943}{908\,328\,960} \right\}, \left\{ \{4, 0, -2\}, \frac{81\,959}{35\,389\,440} \right\}, \\
& \left\{ \{4, 0, 0\}, \frac{11\,016\,701}{4\,087\,480\,320} \right\}, \left\{ \{4, 0, 2\}, \frac{21\,773}{4\,087\,480\,320} \right\}, \left\{ \{4, 2, -4\}, \frac{21\,001}{8\,174\,960\,640} \right\}, \\
& \left\{ \{4, 2, -2\}, \frac{31\,775\,213}{24\,524\,881\,920} \right\}, \left\{ \{4, 2, 0\}, \frac{81\,959}{35\,389\,440} \right\}, \left\{ \{4, 2, 2\}, \frac{294\,541}{6\,131\,220\,480} \right\}, \\
& \left\{ \{4, 4, -4\}, \frac{1}{1\,167\,851\,520} \right\}, \left\{ \{4, 4, -2\}, \frac{21\,001}{8\,174\,960\,640} \right\}, \left\{ \{4, 4, 0\}, \frac{6943}{908\,328\,960} \right\}, \\
& \left\{ \{4, 4, 2\}, \frac{487}{4\,904\,976\,384} \right\}, \left\{ \{5, -1, -3\}, \frac{20\,467}{24\,524\,881\,920} \right\}, \left\{ \{5, -1, -1\}, \frac{264\,307}{6\,131\,220\,480} \right\}, \\
& \left\{ \{5, -1, 1\}, \frac{1663}{1\,362\,493\,440} \right\}, \left\{ \{5, 1, -3\}, \frac{35\,267}{8\,174\,960\,640} \right\}, \left\{ \{5, 1, -1\}, \frac{8\,221\,823}{24\,524\,881\,920} \right\},
\end{aligned}$$

$$\begin{aligned}
& \left\{ \{5, 1, 1\}, \frac{264\,307}{6\,131\,220\,480} \right\}, \left\{ \{5, 3, -3\}, \frac{1007}{24\,524\,881\,920} \right\}, \left\{ \{5, 3, -1\}, \frac{35\,267}{8\,174\,960\,640} \right\}, \\
& \left\{ \{5, 3, 1\}, \frac{20\,467}{24\,524\,881\,920} \right\}, \left\{ \{6, 0, -2\}, \frac{2153}{4\,904\,976\,384} \right\}, \left\{ \{6, 0, 0\}, \frac{1829}{875\,888\,640} \right\}, \\
& \left\{ \{6, 2, -2\}, \frac{1487}{24\,524\,881\,920} \right\}, \left\{ \{6, 2, 0\}, \frac{2153}{4\,904\,976\,384} \right\}, \left\{ \{7, 1, -1\}, \frac{25}{4\,904\,976\,384} \right\} \}
\end{aligned}$$